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Reconstructing the density and temperature structure of prestellar cores from *Herschel* data: A case study for B68 and L1689B

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ABSTRACT

Utilizing multi-wavelength dust emission maps acquired with *Herschel*, we reconstruct local volume density and dust temperature profiles for the prestellar cores B68 and L1689B using inverse-Abel transform based technique. We present intrinsic radial dust temperature profiles of starless cores directly from dust continuum emission maps disentangling the effect of temperature variations along the line of sight which was previously limited to the radiative transfer calculations. The reconstructed dust temperature profiles show a significant drop in core center, a flat inner part, and a rising outward trend until the background cloud temperature is reached. The central beam-averaged dust temperatures obtained for B68 and L1689B are 9.3 ± 0.5 K and 9.8 ± 0.5 K, respectively, which are lower than the temperatures of 11.3 K and 11.6 K obtained from direct SED fitting. The best mass estimates derived by integrating the volume density profiles of B68 and L1689B are $1.6 M_{\odot}$ and $11 M_{\odot}$, respectively. Comparing our results for B68 with the near-infrared extinction studies, we find that the dust opacity law adopted by the HGBS project, $\kappa_{\lambda} = 0.1 \times \left(\frac{\lambda}{300 \mu\text{m}}\right)^{-2} \text{ cm}^2 \text{ g}^{-1}$, agrees to within 50% with the dust extinction constraints.

Key words. ISM: individual objects (Barnard 68, L1689B) – ISM: clouds – ISM: structure – Stars: formation

1. Introduction

Recent submillimeter observations with the *Herschel* Space Observatory (Pilbratt et al., 2010) and particularly the results obtained as part of the *Herschel* Gould Belt Survey (HGBS; André et al., 2010) have significantly improved our global understanding of the early stages of low-mass star formation. It is now becoming clear that the formation of prestellar cores is intimately related to the ubiquitous filamentary structure present in the cold interstellar medium (ISM) (Arzoumanian et al., 2011). One of the main objectives of the HGBS is to measure the prestellar core mass function (CMF) in nearby cloud complexes and to clarify the relationship between the CMF and the stellar initial mass function (IMF) on one hand and the link with the structure of the ISM on the other hand (cf. Könyves et al., 2010; André et al., 2010, for preliminary results).

An accurate determination of the prestellar CMF requires reliable estimates of core masses. In the context of the HGBS project, core masses are derived from dust continuum emission maps obtained with *Herschel* between $160 \mu\text{m}$ and $500 \mu\text{m}$. Dust emission is almost always optically thin at these wavelengths and can thus act as a surrogate tracer of the total (gas + dust) mass along the line of sight (LOS). This requires an assumption about the dust opacity in the submillimeter regime and reliable estimates of the dust temperature, T_d . *Herschel* multi-wavelength data can be used to estimate $\langle T_d \rangle_{\text{LOS}}$ through single-temperature greybody fits to the observed spectral energy distributions (SEDs) (cf. Könyves et al., 2010). A complication, however, is that such fits only provide the average temperature along the LOS and do not account for temperature gradients within the target sources. This is potentially a very significant

problem when studying self-gravitating starless (or protostellar) cores with stratified density structures heated by an external or internal radiation field. The central temperatures of cold, starless cores, and sometimes their mass-averaged temperatures, can be overestimated due to the relatively strong emission from the screen of warmer dust in the outer layers of the cores, biasing core mass estimates to lower values (cf. Malinen et al., 2011). Likewise, temperature variations along the LOS may hamper the derivation of reliable density profiles for prestellar cores (e.g., Kirk et al., 2005; Ysard et al., 2012) using submillimeter emission maps (e.g., Kirk et al., 2005; Ysard et al., 2012). Radiative transfer calculations (e.g., Evans et al., 2001; Stamatellos et al., 2007) have been performed to predict the dust temperature profiles of starless cores whose outer surfaces are exposed to heating by the local interstellar radiation field (ISRF). These calculations generally find a significant drop in T_d at the center of starless cores, but the actual magnitude of this temperature drop remained poorly constrained observationally before the advent of *Herschel* (see Ward-Thompson et al., 2002 for early results with *ISO*, however).

Here, we use *Herschel* observations to quantify the dust temperature gradient within two well-studied starless cores, B68 and L1689B. We introduce a simple yet powerful inversion technique based on the Abel integral transform to simultaneously reconstruct the 3D density and dust temperature profiles of dense cores using as inputs *Herschel* maps in four bands between $160 \mu\text{m}$ and $500 \mu\text{m}$ (also see Marsh et al., 2014 for an independent approach of solving similar problem). The basic goal of the present paper is to demonstrate the performance of the Abel inversion technique. We apply our algorithm to B68

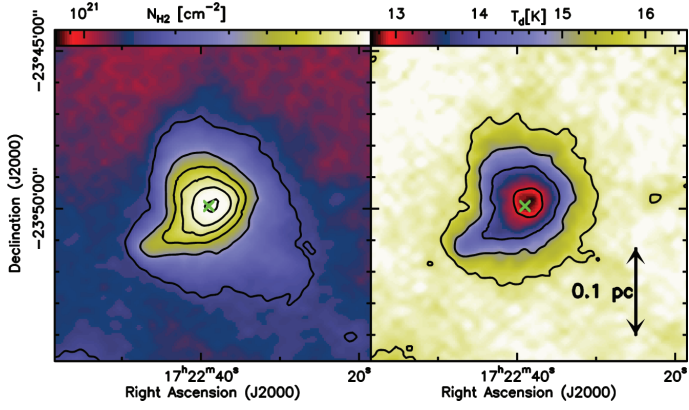


Fig. 1. Column density map (left) and LOS dust temperature map (right) of B68 derived by fitting modified blackbody SEDs to the *Herschel* data between 160 μm and 500 μm on a pixel-by-pixel basis (see Sect. 3.1 for details). The column density contours go from 1.6×10^{21} to 9.6×10^{22} by steps of 1.6×10^{21} in units of H_2 molecules per cm^2 (left), and the temperature contours are 16, 15, 14, 13 K (right). The cross symbol shows the center of the core obtained by fitting a 2D-Gaussian to the column density map.

and L1689B and compare the results with previous infrared extinction/absorption studies, which allows us to validate the dust opacity assumption made in earlier HGBS papers. We also test our technique on synthetic core models with known density and temperature profiles. While the method assumes spherically symmetric cores, we show that it yields satisfactory results for prolate or oblate ellipsoidal cores with realistic aspect ratios $\lesssim 2$.

2. *Herschel* Observations of B68 and L1689B

As a part of the HGBS key project, two fields in the Pipe and Ophiuchus molecular cloud complexes containing B68 and L1689B, of areas $\sim 1.5^\circ \times 1.5^\circ$ and $\sim 3.0^\circ \times 3.5^\circ$ and observed for an integration time of 2.6 and 10.2 hours, respectively. These target fields were mapped¹ in two orthogonal scan directions at a scanning speed of $60'' \text{ s}^{-1}$ in parallel mode, acquiring data simultaneously in five bands with the SPIRE (Griffin et al., 2010) and PACS (Poglitsch et al., 2010) bolometer cameras. The data were reduced using HIPE version 7.0. The SPIRE data were processed with modified pipeline scripts. Observations during the turnaround of the telescope were included, and a destriper module with a zero-order polynomial baseline was applied. The default ‘naïve’ mapper was used to produce the final map. For the PACS data, we applied the standard HIPE data reduction pipeline up to level 1, with improved calibration. Further processing of the data, such as subtraction of (thermal and non-thermal) low-frequency noise and map projection was performed with Scanamorphos v11 (Roussel, 2012). Note that the Scanamorphos map-maker avoids any high-pass filtering which is crucial for preserving extended emission.

3. Description of the Abel inversion method

Consider a spherically symmetric core with radial density profile, $\rho(r)$, embedded in a uniform background and isotropic ISRF.

¹ A more detailed description about the observations and data reductions are also available in the HGBS website: <http://gouldbelt-herschel.cea.fr/archives>.

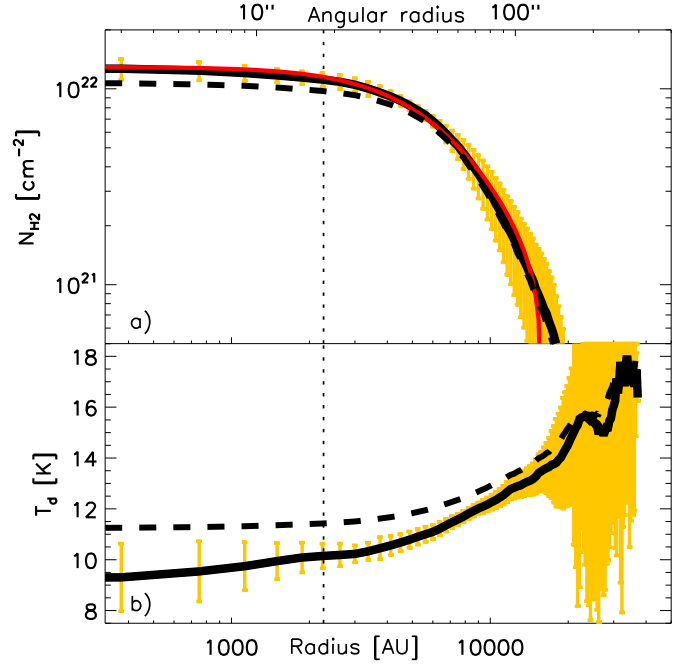


Fig. 2. Column density (a) and dust temperature (b) profiles of B68 obtained at 500 μm resolution by applying the Abel inversion method to the circularly-averaged intensity profiles observed with *Herschel* between 160 μm and 500 μm . **a)** Comparison between the column density profiles derived from the Abel reconstruction (solid black line) and from LOS-averaged SED fitting (thick dashed line). The red curve shows the best-fit Bonnor-Ebert model to the Abel-inverted profile (see Table 2 for parameters). The vertical dotted line represents the half power beam radius of $36''/3/2$ (effective 500 μm resolution). **b)** Comparison of the Abel-inverted (solid line) and LOS-averaged SED (dashed curve) temperature profiles. The error bars represent the standard deviation of $N_{\text{H}_2}(r)$ and $T_d(r)$ values obtained from independent profile reconstructions along sixteen angular directions.

Assuming optically thin dust emission, the specific intensity $I_\nu(p)$ of the core when observed at impact parameter, p , may be expressed as:

$$I_\nu(p) = 2 \int_p^{+\infty} \rho(r) B_\nu[T_d(r)] \kappa_\nu \frac{r dr}{\sqrt{r^2 - p^2}} + I_{\nu,\text{bg}} + I_{\nu,\text{N}}, \quad (1)$$

where $I_{\nu,\text{bg}}$ and $I_{\nu,\text{N}}$ represent the background emission and instrumental noise, respectively, $B_\nu[T_d(r)]$ is the Planck function for the dust temperature $T_d(r)$ at radius r from core center, and κ_ν is the frequency-dependent dust opacity², here assumed to be uniform throughout the core. Given the symmetry of the problem, we can use the inverse Abel transform (e.g. Bracewell, 1986) to obtain the integrand of Eq. (1) at each observed frequency ν :

$$\rho(r) B_\nu[T_d(r)] \kappa_\nu = -\frac{1}{\pi} \int_r^{+\infty} \frac{dI_\nu}{dp} \frac{dp}{\sqrt{p^2 - r^2}}. \quad (2)$$

From Eq. 2, we see that the physical parameters of interest, $\rho(r)$ and $T_d(r)$, only depend on the first derivatives of the radial inten-

² Note the dust-to-gas fraction of 1% is implicitly included in our definition of the dust opacity (see also Sect. 3.1) so that $\rho(r)$ represents the radial gas density of the object.

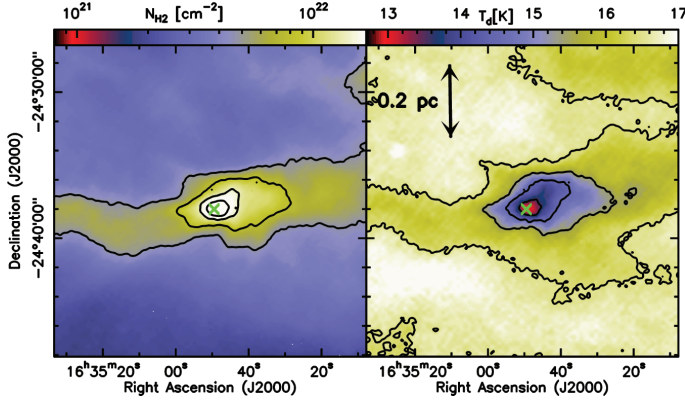


Fig. 3. Same as Fig. 1 but for L1689B. The column density contours are 6×10^{21} , 1×10^{22} , 1.4×10^{22} , 1.8×10^{22} , and 2.6×10^{22} $\text{H}_2 \text{ cm}^{-2}$ (left), and the temperature contours are 16.5, 15.5, 14.5, and 13.5 K (right). The column density image shows that L1689B is embedded inside a filamentary structure.

sity profiles. With a pre-defined assumption about the dust opacity law κ_ν , one may thus estimate $T_d(r)$ at each radius r by fitting a single-temperature modified blackbody to the SED obtained from evaluating the right-hand side of Eq. (2) at each observed band between $160 \mu\text{m}$ and $500 \mu\text{m}$ (see Sect. 3.1 for further details). The density profile, $\rho(r)$, can be derived simultaneously from the normalization of the fit at each radius.

For simplicity, Eq. (1) above neglects the convolution with the telescope beam. However, simulations confirm that beam smearing has little effect in the case of well-resolved cores (see Appendix B). In the case of starless cores such as B68 and L1689B with a flat inner density profile inside a radius R_{flat} , or angular radius θ_{flat} , we find that the beam effect can be parameterized by the ratio $\theta_{\text{flat}}/\text{HPBW}$ (where HPBW is the half-power beam width), and that for $\theta_{\text{flat}}/\text{HPBW} \gtrsim 1$, as is the case for B68 and L1689B, the reconstructed column density profile agrees with the intrinsic profile within 20% (in the absence of noise). More generally, simulations indicate that, in the absence of noise, the reconstructed temperature and column density profiles essentially coincide with the corresponding intrinsic profiles convolved to the effective beam resolution (see Appendix B). Importantly, our Abel inversion technique does not depend on the subtraction of a flat background level as the derivative of a constant background³ does not contribute to the integral of Eq. (2). The reconstruction is, however, quite sensitive to noise fluctuations in the outer parts of the core.

3.1. SED fitting and profile reconstruction

Column density and corresponding LOS-averaged dust temperature maps are shown in Fig. 1 and Fig. 3 for B68 and L1689B, respectively. They were obtained by fitting modified blackbody functions to the *Herschel* SEDs longward of $160 \mu\text{m}$ on a pixel-by-pixel basis as in earlier HGBS papers (Könyves et al., 2010; see also Hill et al., 2011 for HOBYS). While fitting the SEDs, we weighted each data point by the corresponding calibration errors at SPIRE ($\sim 10\%$) and PACS ($\sim 15\%$) wavelengths. Appropriate zero-level offsets were added to each image (see Table 1), obtained by correlating the *Herschel* data with the *Planck* and *IRAS* data of the same fields (see Bernard et al.,

³ If the background is not flat, the input data can be pre-processed by subtracting e.g., a linear plane.

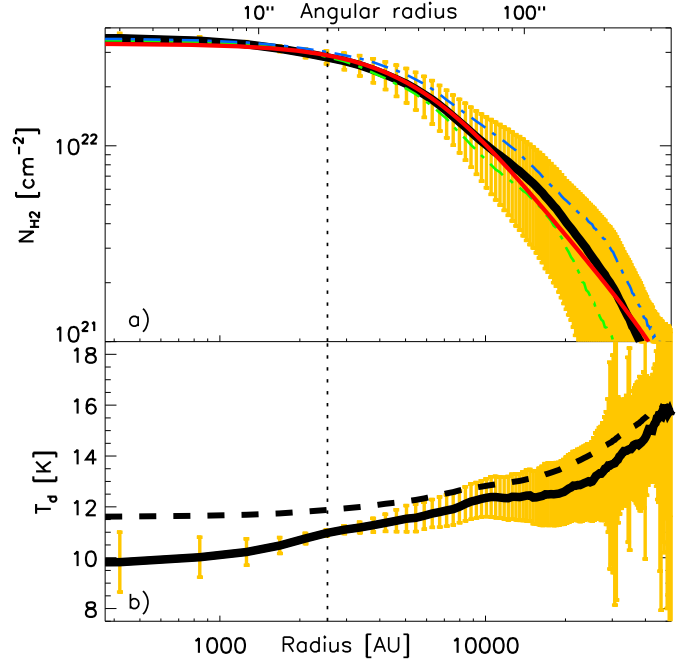


Fig. 4. **a)** Column density profile of L1689B obtained at $500 \mu\text{m}$ resolution by applying the Abel reconstruction method to the circularly-averaged intensity profiles between $160 \mu\text{m}$ and $500 \mu\text{m}$ (black solid curve). The blue and green dash-dotted profiles show the column density profiles obtained from reconstructing the intensity profiles observed along EW and NS sectors, respectively. The overplotted red solid line shows the best-fit Bonnor-Ebert model (see Table 2 for parameters). The vertical dotted line is same as in Fig. 2. **b)** Reconstructed dust temperature profile of L1689B (solid curve) compared with the LOS-averaged temperature profile derived from simple SED fitting (thick dashed curve).

2010). The same dust opacity law as in earlier HGBS (see also Motte et al., 2010 for the HOBYS key program) papers is adopted in the present paper (similar to Hildebrand, 1983): $\kappa_\lambda = 0.1 \times \left(\frac{\lambda}{300 \mu\text{m}}\right)^{-\beta} \text{ cm}^2 \text{ per g}$ (of gas + dust), with a dust emissivity index of $\beta = 2$. Our dust opacity value at the normalizing wavelength is also close to the Ossenkopf & Henning (1994) opacity model for dust grains with thin ice mantles. A mean molecular weight $\mu_{\text{H}_2} = 2.8$ is assumed⁴ to express column density in units of H_2 molecules per cm^2 . Using our adopted dust opacity law, we find that even the central LOSs for B68 and L1689B with $N_{\text{H}_2} \leq 5 \times 10^{22} \text{ cm}^{-2}$ has small optical depths $\lesssim 0.08$ at $160 \mu\text{m}$, confirming that the core emission is optically thin longward of $160 \mu\text{m}$.

The same assumptions have been adopted for the modified blackbody fits required at each radius by the Abel inversion technique. A single-temperature description of the SEDs is suitable in this case because we are sampling local density and dust temperature at a given radius r . Prior to SED fitting, the *Herschel* data are convolved to a common resolution of either $36''.3$ (i.e., HPBW resolution of SPIRE at $500 \mu\text{m}$) or $24''.9$ (i.e., HPBW resolution of SPIRE at $350 \mu\text{m}$, when the $500 \mu\text{m}$ data are not

⁴ Note that this differs from the first HGBS papers (e.g. André et al., 2010; Könyves et al., 2010; Arzoumanian et al., 2011) where $\mu = 2.33$ was assumed and column density was expressed in units of mean free particles per cm^2 .

used). At each wavelength, a circularly-averaged intensity profile about core center is first derived from the *Herschel* data, and the derivative of this average profile is then numerically evaluated and integrated over the kernel shown in the right-hand side of Eq. (2). The central position of the core is obtained from fitting a 2D-Gaussian model to the column density map (see the cross symbols in Fig. 1 and Fig. 3 for B68 and L1689B, respectively). The integration is performed up to an outer radius corresponding to ~ 2 – 2.5 times the *FWHM diameter* of the core as estimated from the 2D-Gaussian fit to the column density map. In practice, the integral on the right-hand side of Eq. (2) converges rapidly and does not depend much on the precise value of the integration outer radius so long as it encompasses the entire core – see Appendix A and Fig. A.1.

3.2. Assessment of uncertainties

The errors bars on the reconstructed profiles at each radius can be estimated from the standard deviations of the density and temperature profiles obtained by repeating the Abel reconstruction along different angular directions around the source (i.e., averaging the data separately over a series of angular sectors instead of circularly-averaging the data). In the case of the reconstructed profiles of B68 and L1689B shown in Fig. 2 and Fig. 4, sixteen equally-spaced angular sectors were used to derive the error bars. The errors we report on the best estimates of the (column) density and temperature at core center correspond to the standard error in the mean, σ/\sqrt{n} , where n is the number of independently measured sectors.

The uncertainty in the normalization of the dust opacity law directly affects the column density estimates but not the temperature estimates, whereas the uncertainty in the emissivity index β influences both the dust temperature and the column density estimates in an anti-correlated fashion. When β is varied from 2 to 1.5, for instance, the dust temperature increases by $\sim 10\%$ and the column density decreases by $\sim 40\%$. The uncertainty in the central position of the core also introduces errors on the derived parameters. To assess the magnitude of this effect in the case of B68, we varied the central position within a radius of $6''$, and found that the resulting central dust temperature and central column density had standard deviations of ± 0.3 K, and $\pm 0.04 \times 10^{22} \text{ cm}^{-2}$, respectively. Besides, departures from spherical symmetry due to, e.g., asymmetries in the density distribution (cf. L1689B in Fig. 3) or an anisotropic background radiation field (cf. Nielbock et al., 2012) may break the symmetry of the quantity $\rho(r)B_\nu(T(r))$ in Eqs. (1) and (2), introducing additional errors. The latter are in principle included in the error bars estimated from the fluctuations of the radial profiles reconstructed along various angular directions. Moreover, we show in Appendix B that cores with moderate departures from spherical symmetry (such as prolate or oblate ellipsoidal cores with aspect ratios $\lesssim 2$) can be reconstructed with reasonable accuracy.

For both B68 and L1689B, the net measurement errors in the derived central T_d and N_{H_2} values are estimated to be ± 0.5 K and $\pm 0.1 \times 10^{22} \text{ cm}^{-2}$, respectively, excluding the systematic uncertainties associated with our assumptions on the dust opacity and the calibration errors. In Appendix B.1 we show that the calibration errors lead to an additional uncertainty of $\sim 12\%$ on column density and $\sim 5\%$ on temperature estimates.

Table 1. Planck offsets in MJy sr^{-1}

Target	160 μm	250 μm	350 μm	500 μm
B68	91.2	77.0	41.6	16.6
L1689B	89.3	136.3	64.4	26.6

4. Detailed results for B68 and L1689B

4.1. B68 core

B68 is a well studied isolated bok globule in the Pipe nebula cloud complex (e.g. Alves et al., 2001; Nielbock et al., 2012). We adopt a distance of 125 pc (de Geus et al., 1989) for the present study. Figure 2 shows the reconstructed column density and temperature profiles obtained from our *Herschel* observations of B68 with the Abel inversion method described in Sect. 3.

In Fig. 2b, the Abel-inverted radial dust temperature profile (solid curve) is compared with the LOS-averaged SED temperature profile (dashed curve). While both temperature profiles exhibit similar features, with a broad minimum around the core center, a positive gradient outside the flat inner plateau of the column density profile, and similar values ($T_d \sim 16.5 \pm 2$ K) at large radii, the minimum Abel-reconstructed temperature at core center is ~ 2 K lower than the minimum SED temperature observed through the central LOS. Accordingly, the central column density derived with the Abel inversion method ($1.3 \pm 0.1 \times 10^{22} \text{ cm}^{-2}$) is 30% higher than the LOS-averaged column density of $\sim 1.0 \times 10^{22} \text{ cm}^{-2}$ derived from standard SED fitting for the central LOS. The difference between the Abel-reconstructed and the LOS-averaged column density becomes negligible in the outer parts of the core. This is indicative of stronger temperature variations along the central LOS compared to the outer LOSs.

Recently, Nielbock et al. (2012) constrained the dust temperature and volume density profiles of B68 using an iterative approach based on 3D radiative transfer modeling of multi-wavelength dust continuum data including *Herschel* observations obtained as a part of the EPoS (Launhardt et al., 2013) key project. They employed a 3-dimensional grid of Plummer-like (Plummer, 1911) density profiles and obtained initial guesses of the parameters from LOS-averaged SED fits. Altogether their model was tuned with eight free parameters, yielding a central dust temperature of $T_d = 8.2^{+2.1}_{-0.7}$ K. The primary reason for the dispersion in the central dust temperature in Nielbock et al. (2012) is the uncertainty of a factor of ~ 2 on the dust opacity in the infrared regime. Although we obtain a higher central dust temperature, $T_d = 9.3 \pm 0.5$ K, with our Abel-inversion method, our results agree with the Nielbock et al. analysis within the range of the quoted uncertainties.

Based on extinction measurements (Alves et al., 2001), the column density profile of B68 closely resembles that of a Bonnor-Ebert (BE) (e.g., Bonnor, 1956) isothermal sphere with a flattened inner region. The overplotted red curve in Fig. 2 shows the best-fit BE model to the reconstructed column density profile. The best-fit BE parameters along with the physical properties that follow directly from the fit such as the radius of the flat inner plateau, $R_{\text{flat}} \equiv 2c_s/\sqrt{4\pi G\rho_c}$, the density contrast, ρ_c/ρ_s , and the external pressure, P_{ext} , are summarized in Table 2. They are consistent with the BE parameters found by Alves et al. (2001).

The N_{H_2} column density profile obtained by integrating the Abel-inverted volume density profile is shown in Fig. 2. This can be directly compared with the near-infrared extinction results Alves et al. (2001) because extinction traces material independently of temperature. For this comparison, we adopted

a standard conversion factor, N_{H_2}/A_V of $9.4 \times 10^{20} \text{ cm}^{-2} \text{ mag}^{-1}$ (Bohlin et al., 1978), to translate column density to equivalent visual extinction A_V at low column densities (i.e., $N_{\text{H}_2} \lesssim 6 \times 10^{21} \text{ cm}^{-2}$). For higher column densities, we used the conversion $N_{\text{H}_2}/A_V = 6.9 \times 10^{20} \text{ cm}^{-2} \text{ mag}^{-1}$ given by Draine (2003), and later on adopted by Evans et al. (2009), consistent with an extinction curve with a total-to-selective extinction, $R_V \equiv A_V/E(B - V) = 5.5$, appropriate in higher density regions.

Using the Bohlin conversion factor, we obtain an A_V of 3.2 mag at a radius of 10^4 AU, agreeing within $\sim 60\%$ with the value of 5 mag reported by Alves et al. (2001) at the same radius. Furthermore, if we correct our estimate for the weak empirical trend between submillimeter dust opacity and column density, $\kappa_\lambda \propto N_{\text{H}_2}^{0.28}$, inferred by Roy et al. (2013) in the regime $1 \lesssim A_V \lesssim 10$ and interpreted as evidence of dust grain evolution, then we find a corrected column density $N_{\text{H}_2}^{\text{corr}} \approx 5 \times 10^{21} \text{ cm}^{-2}$, equivalent to a corrected $A_V^{\text{corr}} = 5.3$ mag, in excellent (10%) agreement with Alves et al. (2001) at 10^4 AU.

Using the Draine conversion factor, we derive an A_V of 19 ± 2 mag through the center of the B68 core compared to the A_V of 30 mag obtained from extinction by Alves et al. (2001), corresponding to a 60% agreement. However, the effective angular resolution of the Alves et al. extinction map was about $\sim 10''$, approximately four times higher than the beam resolution ($36''.3$) of SPIRE at $500 \mu\text{m}$. For better comparison, we performed a similar Abel reconstruction analysis at the beam resolution ($24''.9$) of the SPIRE $350\text{-}\mu\text{m}$ observations, ignoring the $500 \mu\text{m}$ data. In this case, the central Abel-reconstructed column density corresponds to $A_V = 20 \pm 2$ mag, which agrees within 50% with the results of Alves et al. (2001). (The central dust temperature derived at $350\text{-}\mu\text{m}$ resolution coincides within the uncertainties with the $500\text{-}\mu\text{m}$ resolution estimate.)

Likewise, the total mass of $1.6 \pm 0.07 M_\odot$ derived by integrating the Abel-reconstructed density profile of B68 within the outer radius of 1.4×10^4 AU agrees within 30% with the mass of $2.1 M_\odot$ obtained by Alves et al. (2001) from extinction data. For comparison, the mass derived from fitting a modified blackbody to the integrated flux densities is $1.4 \pm 0.05 M_\odot$. The latter does not account for temperature variations along the LOS, and thus slightly underestimates the intrinsic total mass of the core. However, we stress that, for a moderate density core such as B68, the global SED temperature (12.5 ± 0.1 K here) is close to the mass-averaged dust temperature and the SED mass agrees within $\sim 15\%$ with the Abel-reconstructed mass.

Using the above results on the density and temperature structure we can check the energy balance of the B68 core. Assuming optically thin submillimeter emission, a total output luminosity of $0.35 \pm 0.04 L_\odot$ is obtained by integrating the quantity $4\pi \int \rho(r) B_\nu [T_d(r)] \kappa_\nu d\nu$ over the volume of the core. A very similar output luminosity ($0.41 \pm 0.05 L_\odot$) is estimated by integrating the observed SED over wavelengths. These output estimates should be compared to the input luminosity of $\sim 0.40 L_\odot$ provided to the core by the local ISRF (Mathis et al., 1983; with $G_0 \sim 1$), calculated from the total ISRF flux density absorbed⁵ by a spherical object with the same density profile and outer radius as B68 using Eq. 4 of Lehtinen et al. (1998). Note that the above three luminosity values agree with one another.

⁵ The ISRF energy is mostly absorbed at short wavelengths ($0.095 \mu\text{m}$ to $100 \mu\text{m}$). In calculating the absorbed energy we adopted the dust absorption model of Draine (2003) with $R_V = 3.1$.

Table 2. Best-fit parameters of Bonnor-Ebert core models for B68 and L1689B

Source profile	ξ_{max}	ρ_c/ρ_s^a	c_s^b (km s^{-1})	P_{ext} (K cm^{-3}) $\times 10^4$	R_{flat}^c (AU) $\times 10^3$	R_{out} (AU) $\times 10^4$	n_c (cm^{-3}) $\times 10^4$
B68	7.0 ± 0.1	17	0.17	3.9	4.4	1.5	8.3
L1689B-C	16.6 ± 0.7	145	0.27	2.9	4.5	3.7	20
L1689B-NS	13.5 ± 0.3	88	0.24	3.2	4.4	2.9	17
L1689B-EW	16.2 ± 1.7	137	0.26	2.2	4.7	3.8	16.5

^a ρ_c and ρ_s denote central density and density at the outer surface of the BE sphere, respectively

^b Isothermal sound speed

^c Flat inner radius, defined as $R_{\text{flat}} \equiv 2 c_s / \sqrt{4\pi G \rho_c}$

4.2. L1689B

Compared to B68, L1689B is a slightly denser and more centrally condensed core (e.g. André et al., 1996; Bacmann et al., 2000), located in the Ophiuchus complex at a distance of ~ 140 pc. The *Herschel* images reveal that it is embedded within a larger-scale filamentary structure (see Fig. 3). Given the elongated morphology observed in the plane of the sky and the mean apparent aspect ratio ~ 1.3 of the core, the hypothesis of spherical symmetry underlying Eq. (1) is not strictly verified.

In order to assess the validity of our Abel-inversion scheme in this case, we therefore performed test reconstructions for prolate and oblate ellipsoidal model cores with similar aspect ratios. These tests suggest that small departures from spherical symmetry have little impact on the reconstruction results (see Appendix B).

The upper panel of Fig. 4 shows the results of three distinct reconstructions of the column density profile of L1689B, obtained by applying the Abel inversion method to a) the circularly-averaged intensity profiles (thick solid curve), b) the intensity profiles observed in sectors oriented East-West (EW), i.e., approximately along the apparent major axis of the core (blue dash-dotted curve), and c) the intensity profiles observed in sectors oriented North-South (NS), i.e., approximately along the apparent minor axis of the core (green dash-dotted curve). While the three column density profiles agree with each other within the central plateau region, the EW profile lies 30% above the NS profile at large radii $\gtrsim 10^4$ AU, and the circularly-averaged profile is intermediate between the other two. For reference and comparison with B68, a BE model was fitted to each of the three column density profiles and the results of these fits are given in Table 2 (for the sake of clarity, only the model fit to the circularly-averaged intensity profiles is shown in Fig. 4, as a red solid curve). All three fits yield a consistent value for the radius of the flat inner plateau, $R_{\text{flat}} \sim 4500 \pm 100$ AU (corresponding to $\sim 32''$). The average reconstructed column density within R_{flat} is $3.5 \pm 0.1 \times 10^{22} \text{ cm}^{-2}$, in good ($\sim 30\%$) agreement with the H_2 column density averaged over the flat inner part of the core of $4.5\text{--}4.7 \times 10^{22} \text{ cm}^{-2}$ found by Bacmann et al. (2000) based on their ISOCAM mid-infrared absorption study (see their Table 2).

Our best estimate of the total core mass obtained from Abel reconstructing the circularly-averaged intensity profiles is $11 \pm 2 M_\odot$. The tests we performed for ellipsoidal synthetic cores (cf. Appendix B) indicate that the relative error in this mass introduced by the departure from spherical symmetry is less than 4% for an intrinsic aspect ratio of ~ 1.3 . Our mass estimate is in excellent agreement with the total mass reported

by Bacmann et al. (2000). The SED mass derived from fitting a modified blackbody to the integrated flux densities is $7.8 \pm 0.2 M_{\odot}$, i.e., about 30% lower than our best mass estimate. The corresponding global SED temperature of the core is 12.5 ± 0.2 K.

The central dust temperature obtained for L1689B using the Abel transform technique is 9.8 ± 0.5 K (see lower panel of Fig. 4). This value is higher than the very low central dust temperature of 7.5 K advocated by Evans et al. (2001) based on radiative transfer calculations assuming a standard ISRF ($G_0 = 1$). At least part of this discrepancy can be explained by the fact that the effective external radiation field for L1689B is about one order of magnitude stronger than the standard ISRF, due to the presence of early-type stars in the immediate vicinity of the Ophiuchus cloud (cf. Liseau et al., 1999).

5. Conclusions

The results on B68 and L1689B discussed in Sect. 4, along with the tests on model cores presented in Appendix B, demonstrate that the Abel transform technique can successfully produce meaningful radial density and dust temperature profiles for spatially resolved prestellar cores. The most rewarding result is the reconstruction of a radial dust temperature profile directly from *Herschel* dust continuum imaging data, independently of any radiative transfer model. The Abel inversion technique (Sect. 3) is very general, insensitive to background subtraction to first order, and can perform equally well for externally-heated (isotropically) starless cores or internally-heated protostellar cores. While in principle the technique assumes spherically symmetric cores, tests performed on ellipsoidal cores suggest that satisfactory results are obtained even when the hypothesis of spherical symmetry is not strictly valid (such as in the L1689B case – cf. Fig. 3). A similar Abel-transform scheme may also be employed to reconstruct the intrinsic beam-averaged density and temperature profiles of (approximately) cylindrically symmetric filaments from the observed radial intensity profiles averaged along the filament main axes.

For both B68 and L1689B we find a characteristic dip in the dust temperature profile, with minimum beam-averaged values of 9.3 ± 0.5 K and 9.8 ± 0.5 K at core center, respectively. The temperature profile smoothly merges with the background cloud temperature at the outer core radii.

The Abel transform technique yields central beam-averaged H_2 densities of $7.5 \pm 0.5 \times 10^4 \text{ cm}^{-3}$ and $2.0 \pm 0.1 \times 10^5 \text{ cm}^{-3}$ for B68 and L1689B, respectively, corresponding to central column densities of $1.3 \pm 0.1 \times 10^{22} \text{ cm}^{-2}$ and $3.6 \pm 0.1 \times 10^{22} \text{ cm}^{-2}$ after integration of the reconstructed volume density profiles along the LOS. These central column density estimates are approximately 15% larger than the values obtained from direct SED fitting. Comparison of our results with the independent near-IR extinction measurement of the B68 column density profile by Alves et al. (2001) suggests that the dust opacity law adopted by the HGBS consortium, with $\kappa_{300 \mu\text{m}} = 0.1 \text{ cm}^2 \text{ per g}$ (of gas + dust) at $\lambda = 300 \mu\text{m}$ and $\beta = 2$, is accurate to better than (and possibly overestimated by) 50% in the 160–500 μm range for sources of (column) densities comparable to B68 and L1689B. Our adopted opacity value is within $\sim 20\%$ of the value⁶ obtained by Suutarinen et al. (2013) for the dust inside a core of similar column density to the ones considered here. Assuming

that the weak trend between submillimeter dust opacity and column density ($\kappa_{\lambda} \propto N_{H_2}^{0.28}$) found by Roy et al. (2013) at $A_V \lesssim 10$ also holds at higher A_V , we argue that the HGBS dust opacity law may remain valid to within 50% accuracy in the whole range of H_2 column densities between $\sim 3 \times 10^{21} \text{ cm}^{-2}$ and $\sim 10^{23} \text{ cm}^{-2}$.

Since the Abel transformation technique can help us correct the effect of LOS temperature variations on the derivation of total masses, we conclude that the *Herschel* data of the HGBS project hold the promise of delivering core masses to better than a factor of 1.5 to 2 accuracy, at least for spatially-resolved cores.

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⁶ Suutarinen et al., 2013 quote $\kappa_{250 \mu\text{m}} = 0.08 \text{ cm}^2 \text{ g}^{-1}$ with $\beta=2$ and argue that this value is underestimated by 40% inside the core due to temperature variations along the LOS.

Appendix A: Surface brightness profiles and outer radius of B68

The top panel of Fig. A.1 shows the circularly-averaged intensity profiles of the B68 core at SPIRE and PACS wavelengths which were used to construct the column density and temperature profiles shown in Fig. 2. The bottom panel of Fig. A.1 shows the logarithmic slope of the column density profile (black line), defined as $s \equiv d \ln N_{\text{H}_2} / d \ln r$ (dimensionless), as a function of radius. The measured logarithmic slope is $s = 0$ near core center due to flat inner density profile and the finite resolution of the observations. The logarithmic slope profile reaches a minimum value $s_{\text{min}} \sim -1.5$ at $r \sim 10^4$ AU, and goes back to $s \sim 0$ at the outer boundary where the core merges with the slowly-varying background. For comparison, a spherical core with outer density profile $\rho \propto r^{-2}$ would have $s = -1$ at large radii. In the same plot we show the logarithmic slope of the $500 \mu\text{m}$ surface brightness profile (blue line) which has a shallower slope due to the additional effect of the positive outward temperature gradient. Inspection of the intensity and slope profiles shown in Fig. A.1 allowed us to select an appropriate upper integration radius in the right-hand side of Eq. (2) when reconstructing the density and temperature structure of B68 (see Sect. 3). Since $\frac{dl_v}{dp} = s \times \frac{l_v}{p} \approx 0$ beyond a radius ~ 25000 AU, larger radii do not contribute to the integral of Eq. (2). In practice, we adopted an upper integration radius $R_{\text{up}} = 37500$ AU for B68, as shown by the dashed vertical line in Fig. A.1. The reconstruction results, however, are insensitive to the precise choice of R_{up} as long as $R_{\text{up}} \gtrsim 25000$ AU. The adjacent dot-dashed vertical line shows the effective radius of ~ 27000 AU (or $\sim 200''$) derived by the *getsources* source-finding algorithm for the ‘footprint’ of B68. The *getsources* algorithm (Men’shchikov et al., 2012) is the source extraction method used by the HGBS consortium to produce the first-generation catalogs of dense cores found by *Herschel* in the regions covered by the HGBS survey. The footprint of a core corresponds to the area just outside of which *getsources* estimates the local background emission and over which it integrates the background-subtracted emission to derive the total flux densities of the core. In the case of B68, the results automatically derived by *getsources* are in excellent agreement with those obtained through a detailed radial profile analysis (cf. Fig. A.1).

Appendix B: Tests of the Abel inversion method using simple models

B.1. Spherically symmetric core model

In order to test the performance level of our Abel inversion scheme and quantify the robustness of the reconstruction, we applied the algorithm described in Sect. 3 to synthetic images corresponding to model starless cores of known density and temperature distributions. First, we considered a spherically-symmetric core model with a Plummer-type density distribution for $r \leq R_{\text{out}}$,

$$\rho(r) = \frac{\rho_c}{1 + (r/R_{\text{flat}})^2}, \quad (\text{B.1})$$

parameterized by physical parameters approximately similar to the derived properties of B68 (see Sect. 4.1): central H_2 number density $n_c \equiv \rho_c / \mu_{\text{H}_2} m_{\text{H}} = 8 \times 10^4 \text{ cm}^{-3}$; flat inner radius R_{flat}

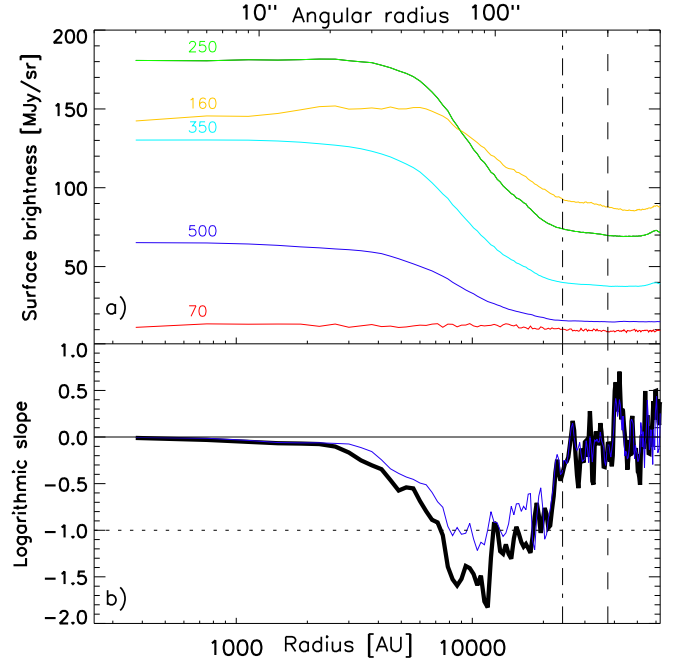


Fig. A.1. **a)** Circularly-averaged radial surface brightness profiles of B68 at 70, 160, 250, 350, 500 μm derived from *Herschel*/SPIRE and PACS data (after adding Planck offsets). **b)** Logarithmic slopes of the circularly-averaged column density profile (black solid curve) and 500 μm intensity profile (blue solid curve) of B68 as a function of radius. The horizontal dotted line is the logarithmic slope $s = -1$ expected for the column density profile of a core with a $\rho \propto r^{-2}$ density profile. The vertical dashed line marks the integration upper bound adopted when integrating the right-hand side of Eq. 2 to perform the Abel reconstruction of the density and temperature profiles (see Sect. 3). The vertical dot-dashed line shows the radius of the footprint automatically derived for B68 by the *getsources* source-finding algorithm.

$= 5 \times 10^3$ AU, and outer radius $R_{\text{out}} = 1.5 \times 10^4$ AU. The surface density profile of such a model core has an analytical form:

$$\Sigma(p) = \frac{2\rho_c R_{\text{flat}}}{(1 + p^2/R_{\text{flat}}^2)^{1/2}} \times \tan^{-1} \left(\frac{(R_{\text{out}}^2 - p^2)^{1/2}}{(R_{\text{flat}}^2 + p^2)^{1/2}} \right), \quad (\text{B.2})$$

where p represents the impact parameter from core center in the plane of the sky, and $N_{\text{H}_2}(p) = \Sigma(p) / \mu_{\text{H}_2} m_{\text{H}}$ is the H_2 column density profile. The intrinsic density profile of the model is shown as a black solid curve in Fig. B.1a, and the corresponding column density profile as a black solid curve in Fig. B.1b. The synthetic dust temperature profile is shown as a black solid curve in Fig. B.1c and was obtained for a solar-neighborhood ISRF ($G_0 = 1$) using an analytic approximation formula reproducing a grid of spherically symmetric models performed with the dust radiative transfer code MODUST (Bouwman et al. 2013, *in preparation* – see Bouwman et al., 2001 and André et al., 2003).

A set of synthetic emission maps was created by line-of-sight integration of this model core at all *Herschel* wavelengths assuming optically thin dust emission (see Eq. 1) and the same dust opacity law as given in Sect. 3.1. The density and temperature profiles of the model core were then reconstructed as described in Sect. 3 from the circularly-averaged radial intensity

profiles of the model emission. The cross symbols overlaid on the model density, column density, and temperature profiles in Figs. B.1a,b,c show the Abel-reconstructed profiles that would be obtained with “infinite” angular resolution (and in the absence of noise). It can be seen in Fig. B.1 that, in this case, the reconstruction is perfect, demonstrating the validity of our Abel-inversion code. The overplotted red curves in Figs. B.1a,b,c show the reconstructed volume density, column density, and temperature profiles resulting from the Abel-inversion method after convolution of the model images to a common resolution of $36''.3$ corresponding to the *Herschel* resolution at $500\text{ }\mu\text{m}$. Likewise, the overplotted blue curves in Figs. B.1a,b,c show the results obtained at a resolution of $24''.9$, using the synthetic data convolved to the *Herschel* resolution at $350\text{ }\mu\text{m}$ and ignoring the $500\text{ }\mu\text{m}$ data. It can be seen that the profiles reconstructed at the *Herschel* resolution remain in excellent (1%) agreement with the intrinsic profiles in the outer part of the core. Although the reconstruction becomes somewhat inaccurate below the *Herschel* resolution limit (marked by vertical dotted lines in Figs. B.1), the reconstructed column density and temperature profiles still agree with the corresponding intrinsic profiles to within 20% and 9%, respectively, at $500\text{ }\mu\text{m}$ resolution. The accuracy of the results at small radii improves to 11% and 5% when the reconstruction is performed at $350\text{ }\mu\text{m}$ resolution (although in the presence of noise with real data, the statistical measurement uncertainties are somewhat larger at $350\text{ }\mu\text{m}$ resolution). At both resolutions, the Abel-reconstructed temperature and column density profiles coincide within 1% with the corresponding intrinsic profiles *convolved* with the effective beam resolution. The reconstructed central temperature and column density thus provide excellent estimates of the beam-averaged central temperature and column density in the model. The total mass estimated by integrating the reconstructed column density profile agrees with the model mass to better than 0.1% even at $500\text{ }\mu\text{m}$ resolution.

We also assessed the contribution of background fluctuations and calibration errors to the uncertainties in the derived parameters (N_{H_2} and T_d). To do so, we considered 500 realizations of synthetic skies including a random Gaussian noise component⁷, σ_v , and a random multiplicative calibration factor, $(1 + g)$:

$$I_v^{\text{sim}}(x, y) = [I_v^{\text{model}}(x, y) + \sigma_v](1 + g), \quad (\text{B.3})$$

where, g is a Gaussian random number with mean zero and standard deviation of 10% and 15% at SPIRE and PACS wavelengths, respectively. (We assumed 100% correlated calibration errors at SPIRE wavelengths and an independent calibration error in the PACS $160\text{ }\mu\text{m}$ band.) The net uncertainties in n_{H_2} , N_{H_2} , and T_d were estimated to be 15%, 12%, and 5%, respectively. The resulting $1\text{-}\sigma$ errors in the derived parameters are displayed in Fig. B.1.

B.2. Ellipsoidal core model

As real cores such as L1689B are often elongated and thus not strictly spherically symmetric (see Sect. 4.2), we also tested the reliability of our Abel inversion scheme using a simple non-spherical model with an ellipsoidal Plummer-like density distribution for $r \leq R_{\text{out}}$ and $z \leq Z_{\text{out}}$, with cylindrical symmetry about the z axis (assumed to lie in the plane of the sky):

$$\rho(r, z) = \frac{\rho_c}{1 + (r/R_{\text{flat}})^2 + (z/Z_{\text{flat}})^2}, \quad (\text{B.4})$$

⁷ The level of noise fluctuations (σ_v) was chosen so that the peak signal-to-noise $I_v^{\text{peak}}/\sigma_v$ value at each wavelength was consistent with the corresponding B68 surface brightness image.

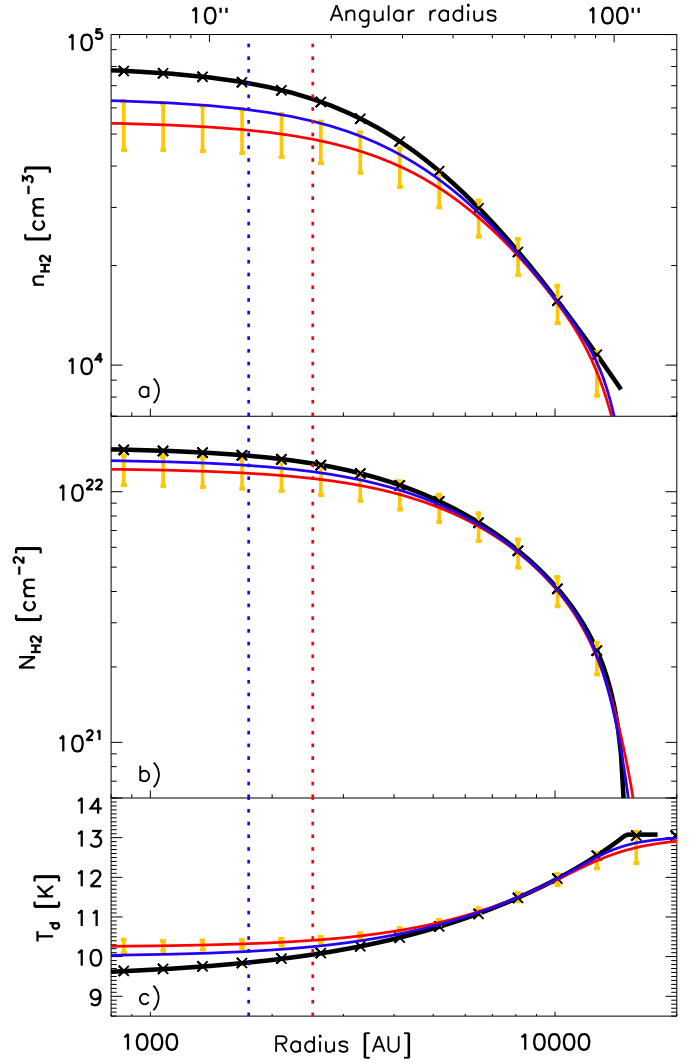


Fig. B.1. Comparison between intrinsic (black curves) and reconstructed (red and blue curves) volume density (a), column density (b), and dust temperature (c) profiles for a spherically symmetric core model with a Plummer-like density distribution (see Eq. B.1 and text for model parameters). The cross symbols show the results obtained by applying the Abel reconstruction scheme on the synthetic $160\text{--}500\text{ }\mu\text{m}$ intensity profiles with “infinite” resolution. The red and blue curves show the reconstruction results obtained from synthetic emission maps smoothed to HPBW resolutions of $36''.3$ and $24''.9$, respectively, corresponding to the resolutions of *Herschel* $500\text{ }\mu\text{m}$ and $350\text{ }\mu\text{m}$ observations. Note the good agreement between the reconstructed profiles and the intrinsic profiles beyond the half power beam radius of $36''.3/2$ ($500\text{ }\mu\text{m}$ resolution) or $24''.9/2$ ($350\text{ }\mu\text{m}$ resolution), marked by the red and blue vertical dotted lines, respectively. The error bars in each panel show the $1\text{-}\sigma$ uncertainties due to random noise and calibration errors.

where R_{flat} and Z_{flat} are the radii of the flat inner core region perpendicular and parallel to the z axis of symmetry (see Fig. B.2a), respectively. We considered both the prolate ($Z_{\text{flat}} > R_{\text{flat}}$) and the oblate ($Z_{\text{flat}} < R_{\text{flat}}$) configuration, but are primarily describing the prolate case here as it is more likely for cores embedded within filaments such as L1689B (see Fig. 3). The synthetic tem-

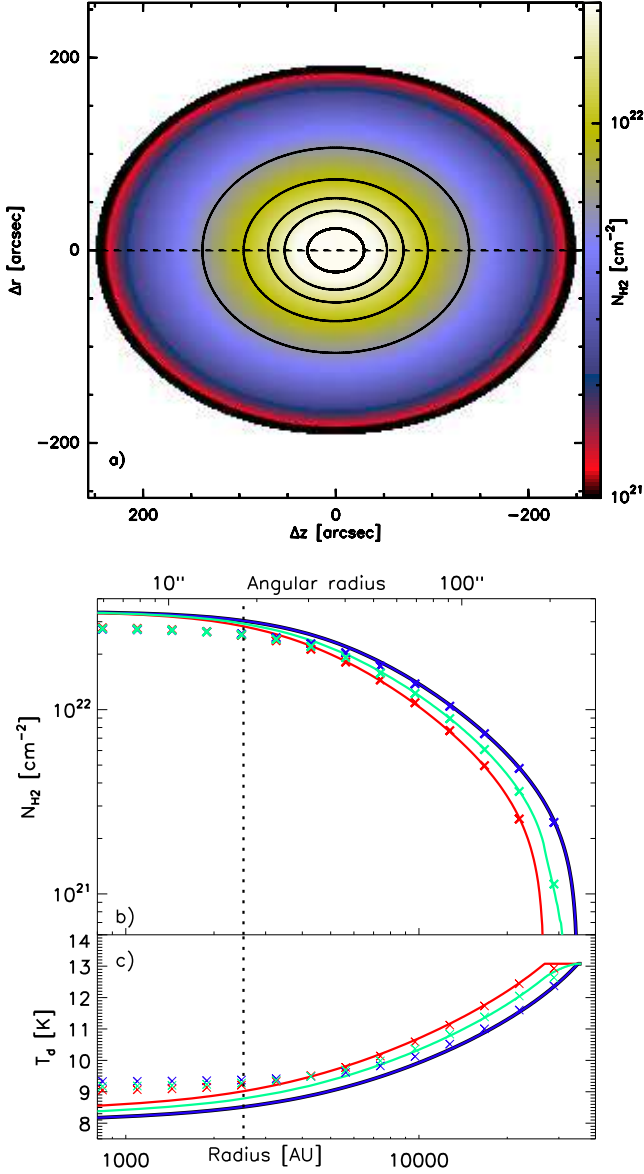


Fig. B.2. (a) Synthetic column density image of a prolate ellipsoidal core model with an aspect ratio of 1.3 and a Plummer-like density distribution (see Eq. (B.4) and the text for model parameters). The horizontal dotted line shows the axis of symmetry in the plane of sky and the contour levels are same as in Fig. 3. (b) Comparison between the intrinsic (solid curves) and the reconstructed (crosses) column density profiles of the model. (c) Comparison between the intrinsic (solid curves) and the reconstructed (crosses) dust temperature profiles of the model. The blue and red curves represent the intrinsic radial profiles along and perpendicular to the axis of symmetry, respectively. The green curves represent the intrinsic circularly-averaged radial profiles. The blue and red crosses display the results of the Abel-inversion method applied to the synthetic 160–500 μm intensity profiles of the model convolved to $36''.3$ resolution and taken along the major and minor axes, respectively. The green crosses show the reconstruction results using the circularly-averaged intensity profiles of the model as inputs. Note the good agreement between the reconstructed profiles and the intrinsic profiles beyond the half power beam radius of $36''.3/2$, marked by the vertical dotted line.

perature distribution was also assumed to be cylindrically symmetric about the z axis and was constructed using the same grid of MODUST radiative transfer models as in Sect. B.1. The synthetic temperature profiles along both the z axis and the radial (r) direction are shown in Fig. B.2. For direct comparison with L1689B (see Fig. 3 and Fig. B.2a), we adopted physical parameters approximately consistent with the observed characteristics of the L1689B core (see Sect. 4.2): central H_2 number density $n_c = 2 \times 10^5 \text{ cm}^{-3}$; aspect ratio $Z_{\text{flat}}/R_{\text{flat}} = Z_{\text{out}}/R_{\text{out}} = 1.3$; flat inner radius along the minor axis $R_{\text{flat}} = 4000 \text{ AU}$; outer radius along the minor axis $R_{\text{out}} = 6.7 \times R_{\text{flat}} = 26800 \text{ AU}$.

Because of the lack of spherical symmetry we applied our Abel reconstruction scheme to three sets of intensity profiles: 1) the profiles measured along the major axis of the model (intrinsic profiles shown as blue curves and results as blue crosses in Fig. B.2); 2) the profiles measured along the minor axis of the model (intrinsic profiles shown as red curves and results as red crosses in Fig. B.2); and 3) circularly-averaged intensity profiles (intrinsic profiles shown as green curves and results as green crosses in Fig. B.2). Here, again, it can be seen that the reconstruction results are very satisfactory (2% agreement) beyond the beam radius (marked by the vertical dotted line in Fig. B.2). The reconstruction performed perpendicular to the axis of symmetry, i.e., along the minor axis for a prolate core, is more accurate (1%) than the reconstruction performed along the axis of symmetry (4%). In particular, the best estimate of the central dust temperature is obtained from the reconstruction performed along the minor axis. The reconstruction along the major axis nevertheless provides better estimates of the column density and temperature at large radii along the major axis. The central column density reconstructed at 500 μm resolution slightly underestimates, but still agrees to within 20% with, the true column density at core center. The best estimate of the total core mass, obtained by using the results of the reconstruction performed on the circularly-averaged intensity profiles, agrees to better than 4% with the model core mass. Even for a more elongated core model with an aspect ratio of 2 (instead of 1.3), the reconstructed core mass still agrees with the model mass to within 5%.

We also performed similar simulations for an oblate core model observed edge-on. The accuracy of the reconstruction results was found to be essentially the same as for the prolate case. Again, the reconstruction performed perpendicular to the axis of symmetry, i.e., along the major axis in this case, was found to be more accurate than the reconstruction performed along the axis of symmetry. The best estimate of the total core mass was

again obtained from reconstructing the circularly-averaged intensity profiles.

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